
$$1+1+1 = 4 \text{ ?}^*$$

* (for larger values of 1)

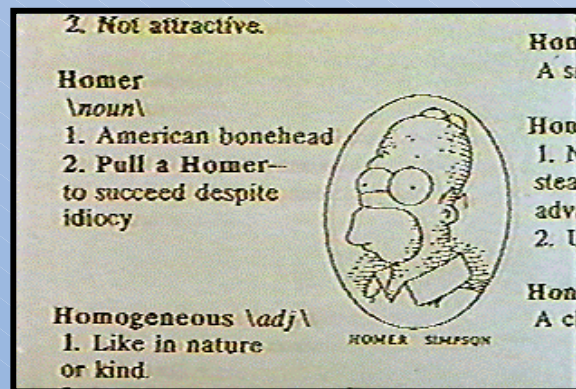
Masses, Mixings, and Sterile Neutrinos

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(My) Skill Level...



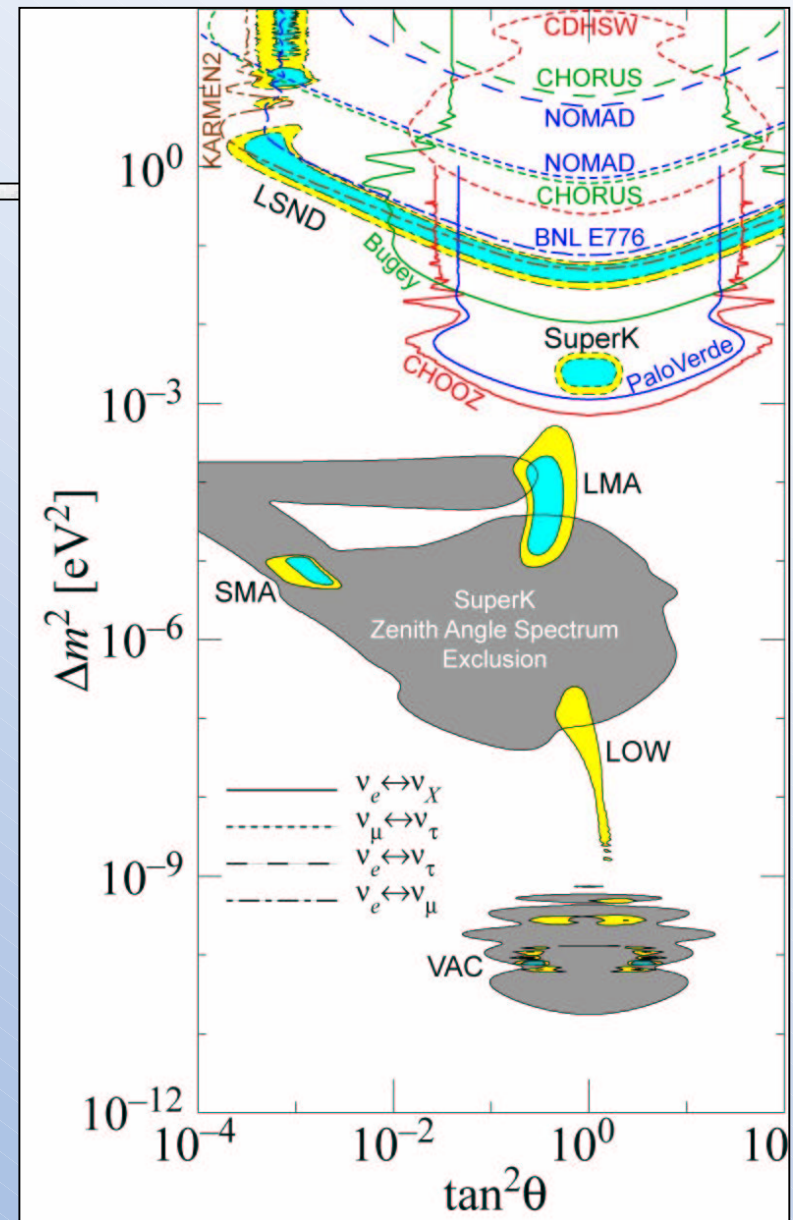
...Experiment



...Theory

Beyond a Reasonable Doubt...

- Our understanding of neutrinos has changed in light of new evidence:
- Neutrinos no longer massless particles (though mass is very small)
- Experimental evidence from three different phenomena:
 - Solar
 - Atmospheric
 - Accelerator
- Data supports the interpretation that neutrinos *oscillate*.

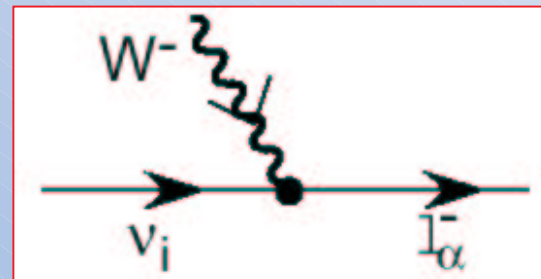


The Standard Model

- Mirror to the quarks, leptons can be sub-divided into families...
- ...which propagate via the exchange of the weak force
- ...and can be graphically be expressed as an exchange of W/Z bosons.

<i>Family:</i>	1	2	3
<i>Leptons</i>	$\begin{pmatrix} e \\ \nu_e \end{pmatrix}_L$	$\begin{pmatrix} \mu \\ \nu_\mu \end{pmatrix}_L$	$\begin{pmatrix} \tau \\ \nu_\tau \end{pmatrix}_L$
	$(e)_R$	$(\mu)_R$	$(\tau)_R$

$$L_{l\nu W} = \frac{-g}{\sqrt{2}} \sum_{\substack{\alpha=e,\mu,\tau \\ i=1,2,3}} \bar{l}_{L\alpha} \gamma^\lambda U_{\alpha i} \nu_{Li} W_\lambda^- + \frac{-g}{\sqrt{2}} \sum_{\substack{\alpha=e,\mu,\tau \\ i=1,2,3}} \bar{\nu}_{Li} \gamma^\lambda U_{i\alpha}^\dagger l_{L\alpha} W_\lambda^+$$




Mixing

- Just as in the quark sector, it is possible to define a *Lepton Mixing Matrix* (Maki-Nakagawa-Sakata-Pontecorvo)

MNSP Matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

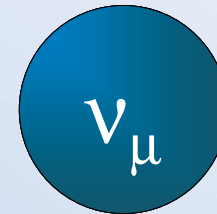
- Relates ν mass eigenstates to weak eigenstates
- For the Standard Model, there is no mixing...


$$U_{\alpha i} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Neutrino Oscillations

If neutrinos have mass then the lepton mixing matrix (MNSP) is expressed as

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



and flavor eigenstates are a mixture of mass eigenstates.

Then

$$\nu_e = U_{e1}\nu_1 + U_{e2}\nu_2 + U_{e3}\nu_3$$

and the state evolves with time or distance

$$\nu_e = U_{e1}e^{-iE_1t}\nu_1 + U_{e2}e^{-iE_2t}\nu_2 + U_{e3}e^{-iE_3t}\nu_3$$

where $E_i^2 = p^2 + m_i^2$

$$P_{e\mu} \sim \sin(2\theta) \sin^2(1.27 \Delta m^2 L / E)$$

- Physics:

Δm^2 & $\sin(2\theta)$

- Experiment:

Distance (L) & Energy (E)

Steriles: Theoretical Motivation

- **Unresolved Questions:**

- Why are neutrino masses so small?
- Why are neutrinos seen only as left-handed particles? Is this compatible with neutrino mass at all?
- Can neutrino mass tell us what is going on at a much higher energy scale?

ϕ_L only

- **Sterile Neutrinos:**

- Can be invoked as right-handed partners to the neutrino
- Naturally introduce mass into the (extended) SM and extend symmetry to quarks

$$\mathcal{L} = m_D(\bar{\psi}_R\psi_L + \bar{\psi}_L\psi_R)$$

- Arise naturally from more comprehensive theories (Grand Unified Theories, etc.)

ϕ_L and ϕ_R

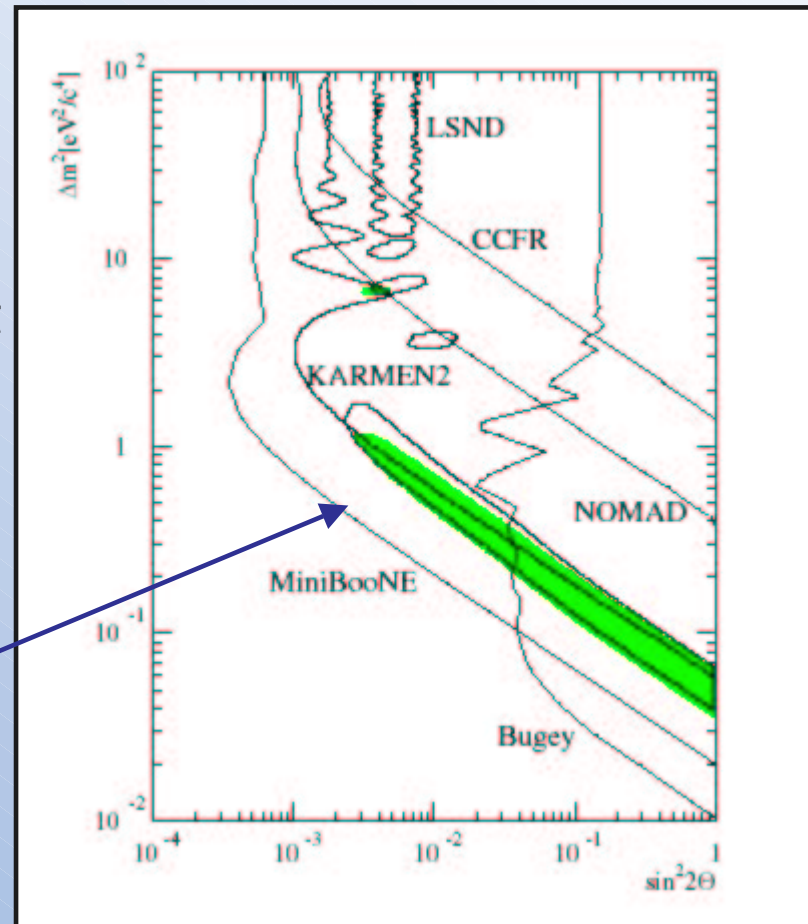
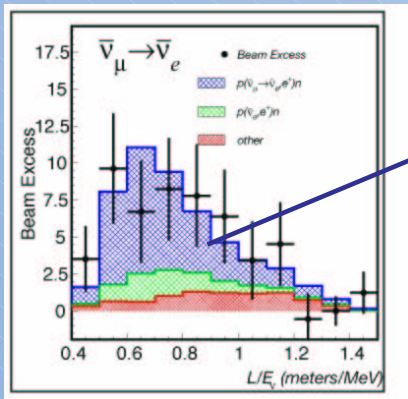
Beyond the Standard Model

- It is possible to introduce heavy neutral leptons (“sterile” neutrinos) into the Standard Model
- Steriles exhibit certain properties in common with ordinary neutrinos:
 - Massive, potentially unstable
 - No electromagnetic couplings
 - No strong couplings
 - No direct weak couplings !
- No strong, no electromagnetic, no weak... no problem !

Steriles: Experimental Motivation

- LSND sees oscillation signal $\bar{\nu}_\mu$ to $\bar{\nu}_e$
- Combined analysis with KARMEN2 experiment consistent with $\Delta m^2 < 1 \text{ eV}^2$

Oscillation Probability:
(0.264±0.067±0.045)%



E. Church, K. Eitel, G. Mills, M. Steidl
hep/ex 0203023

Doesn't Add Up

- If dealing with 3 neutrino species then...

$$\Delta m_{12}^2 + \Delta m_{23}^2 + \Delta m_{31}^2 = 0$$

- But if Δm_{12}^2 and Δm_{23}^2 are both small then Δm_{31}^2 must be small as well (constrained).
- ...but this is not the case.

$$\Delta m_{\text{solar}}^2 = (4.0 - 9.0) \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{\text{atm}}^2 = (1.6 - 3.9) \times 10^{-3} \text{ eV}^2$$

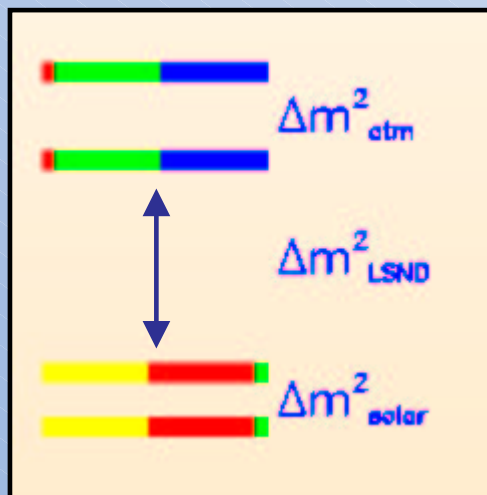
$$\Delta m_{\text{LSND}}^2 = (0.1 - 1.0) \times 10^0 \text{ eV}^2$$

- How do we constrain something we cannot see?

Two Phenomenological Models

- **2+2 Model:**

- Assumes mass difference of LSND signal bridges between solar and atmospheric

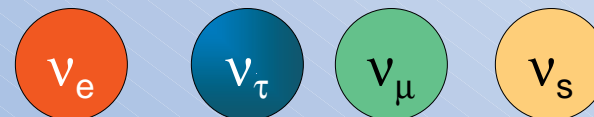
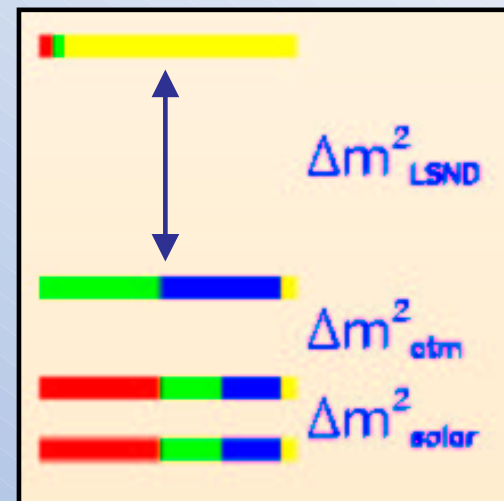


- Model gives prediction of:

$$P_{\text{solar}} + P_{\text{atmo}} = 1$$

- **3+1 Model:**

- Assumes LSND mass apart from near degenerate weak states.



Testing the Sterile Content

- Using Solar & Reactor:
 - Direct measurement of ^8B flux from sun from SNO measurement
 - Use SNO + KamLAND to further constrain solar models
 - Use lowest energy solar ν 's to understand steriles
- Global Fits:
 - Use combined fits to constrain 2+2 and 3+1 predictions
 - Determine if ν_μ to ν_τ really occurs
- “Direct” Measurement:
 - MiniBooNE

Sudbury Neutrino Observatory

2092 m to Surface (6010 m w.e.)

PMT Support Structure, 17.8 m
9456 20 cm PMTs
~55% coverage within 7 m

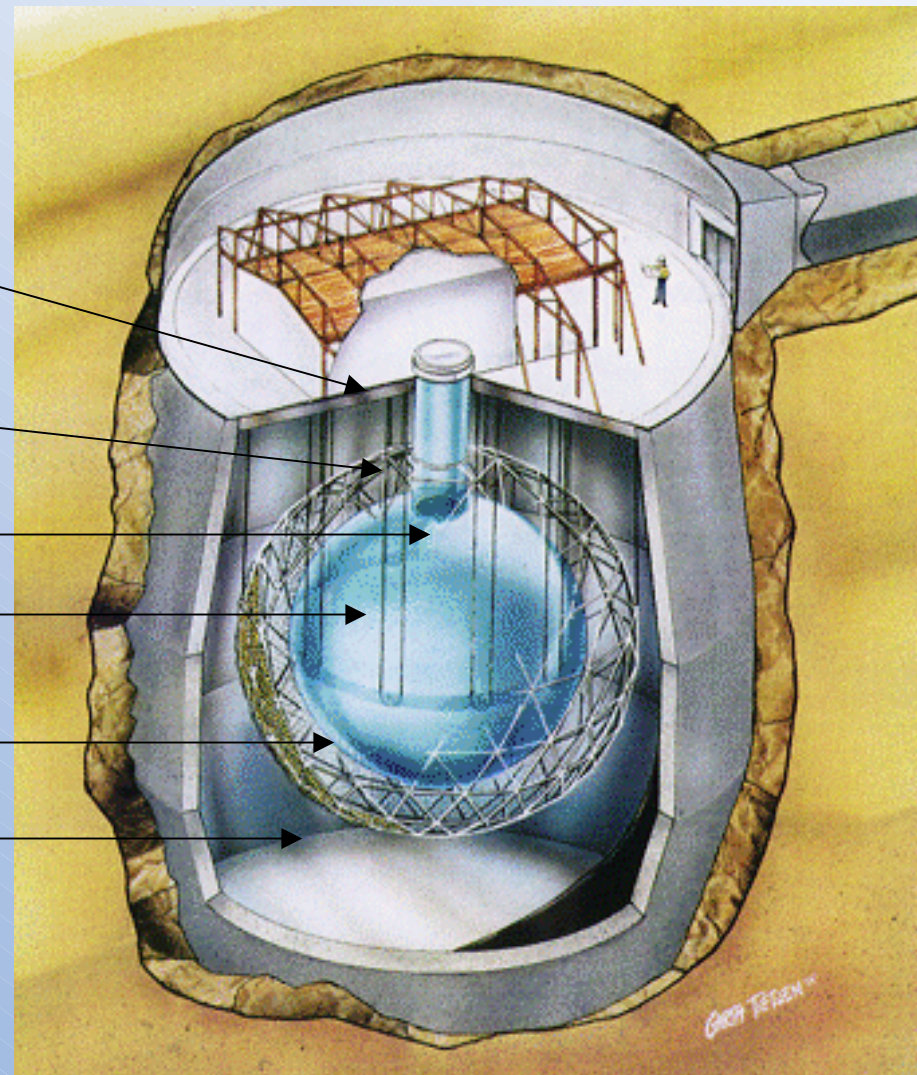
Acrylic Vessel, 12 m diameter

1000 Tonnes D_2O

1700 Tonnes H_2O , Inner Shield

5300 Tonnes H_2O , Outer Shield

Urylon Liner and Radon Seal



Unique Experiment

- Since only ν_e 's are produced in the sun, ideal to measure the electron and non-electron solar flux in one single experiment.

Charged-Current (CC)

$$\nu_e + d \rightarrow e^- + p + p$$

$$E_{\text{thresh}} = 1.4 \text{ MeV}$$

ν_e only

Signature: ^8B energy spectrum

Measurement of energy spectrum

Elastic Scattering (ES)

$$\nu_x + e^- \rightarrow \nu_x + e^-$$

ν_x , but enhanced for ν_e

Strong directional sensitivity

Neutral-Current (NC)

$$\nu_x + d \rightarrow \nu_x + n + p$$

$$E_{\text{thresh}} = 2.2 \text{ MeV}$$

ν_x

Signature : mono-energetic γ

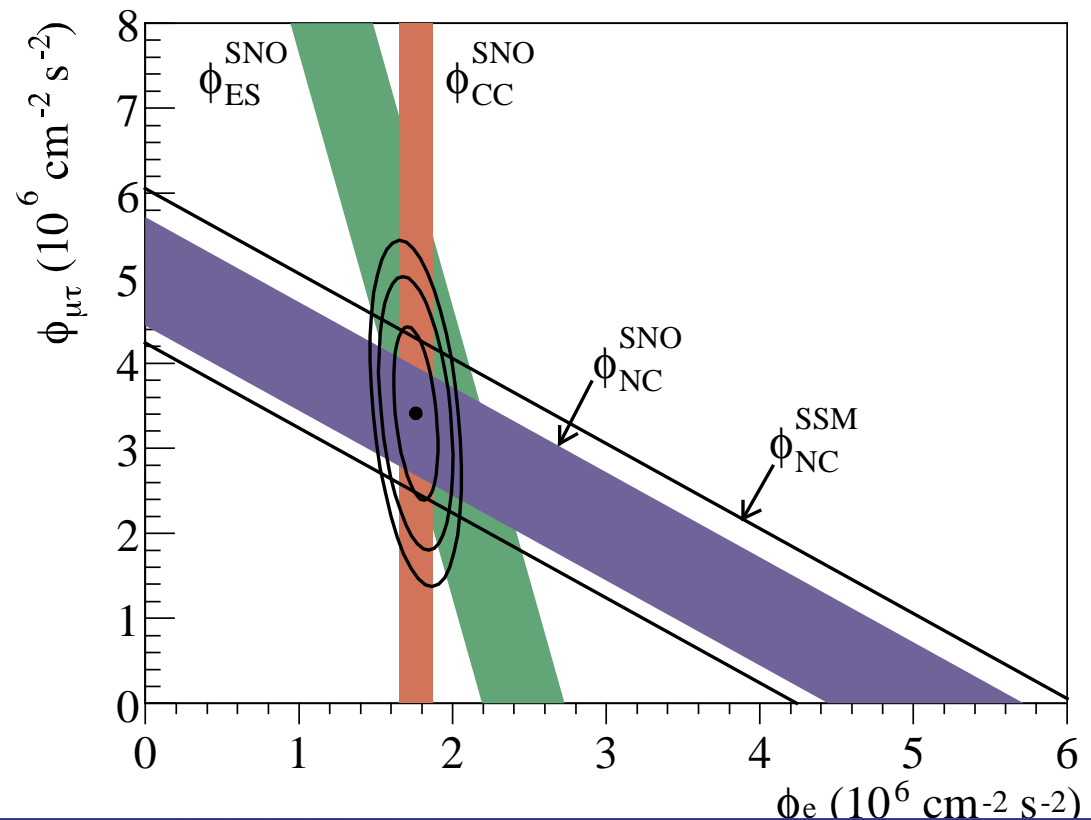
Measures total ^8B flux from Sun

Solar Physicists Were Right!

- Measurement of ^8B flux from the sun.
- Final flux numbers:

$$\Phi_{\text{SSM}}^{8\text{B}*} = 5.05 \quad \begin{matrix} +1.01 \\ -0.81 \end{matrix}$$

$$\Phi_{\text{SNO}}^{\text{NC}*} = 5.09 \quad \begin{matrix} +0.44 & +0.46 \\ -0.43 & -0.43 \end{matrix}$$



* in units of $10^6 \text{ cm}^{-2} \text{ s}^{-1}$

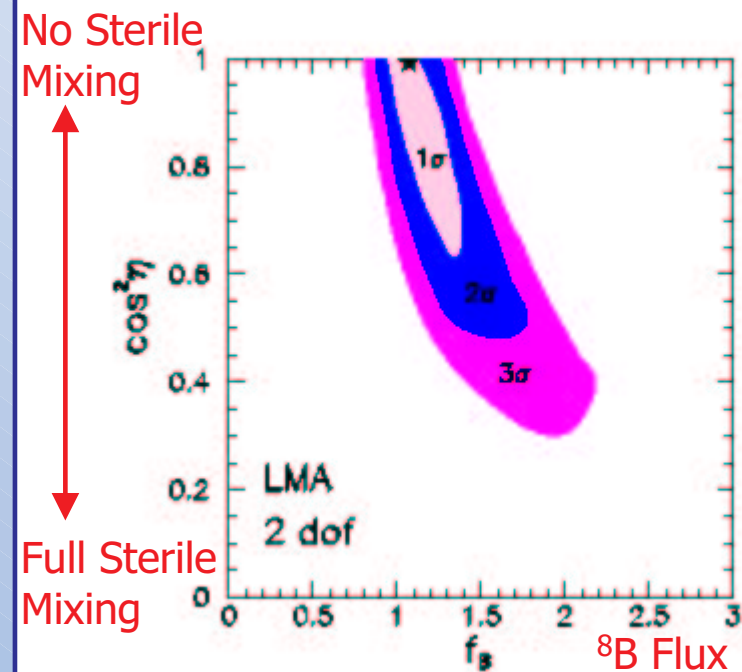
What About Sterile Neutrinos?

- Best fit favors no oscillations to sterile neutrinos
- Pure mixing $\nu_e \rightarrow \nu_s$ ruled out at the 5σ level
- Partial mixing (global fit) of mixing parameter to steriles (η):

$$\sin^2 \eta < 0.70 \quad (3\sigma)$$

- What is the problem?
 - Sterile content driven by uncertainties in the flux. Is there a way to constrain it further?

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hep/ph 0204194



KamLAND

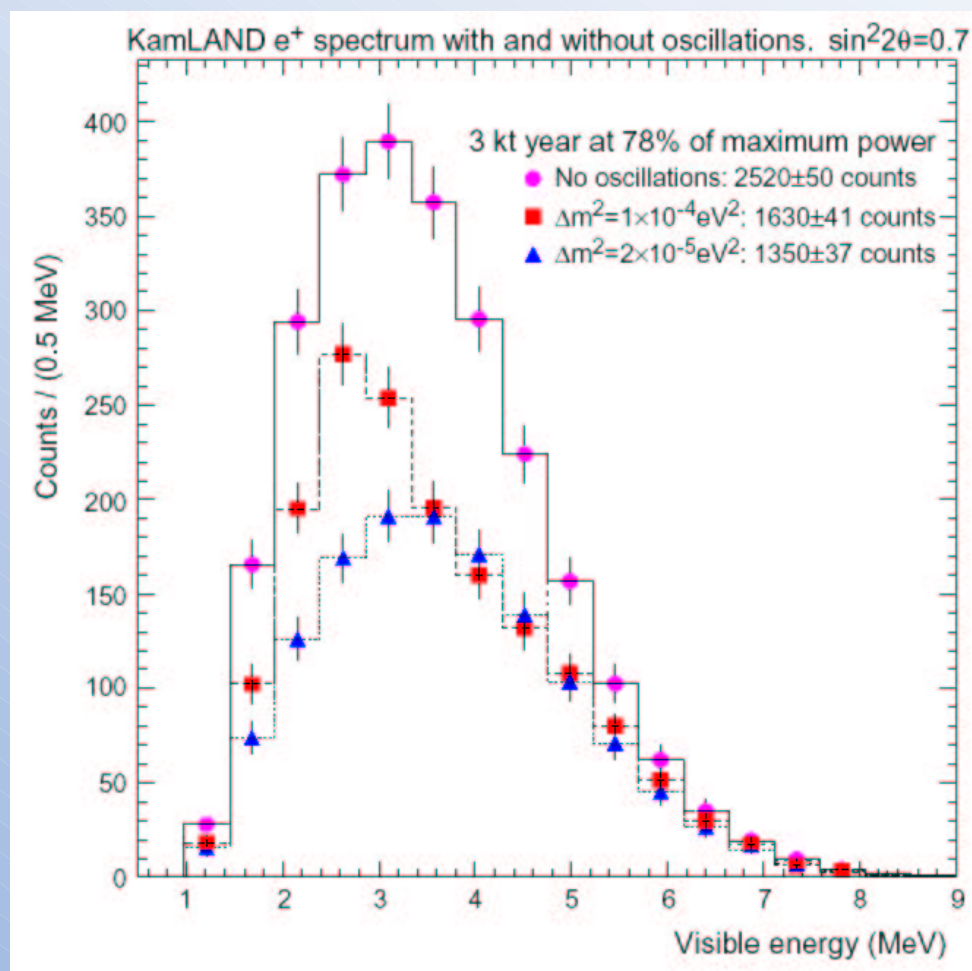
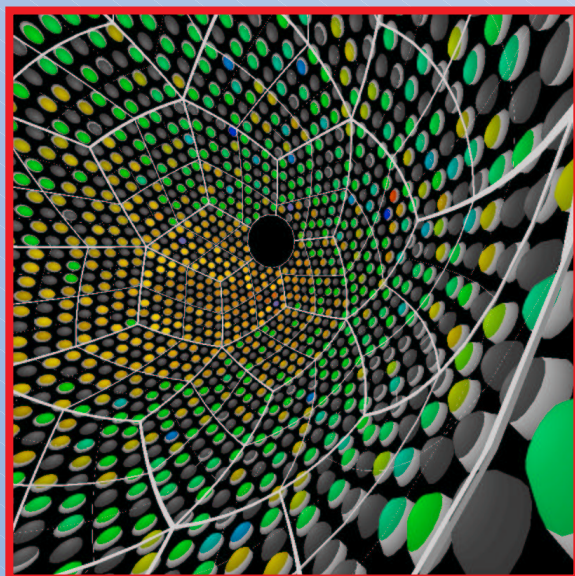
KamLAND

Kamioka

Liquid scintillator

Anti-Neutrino

Detector



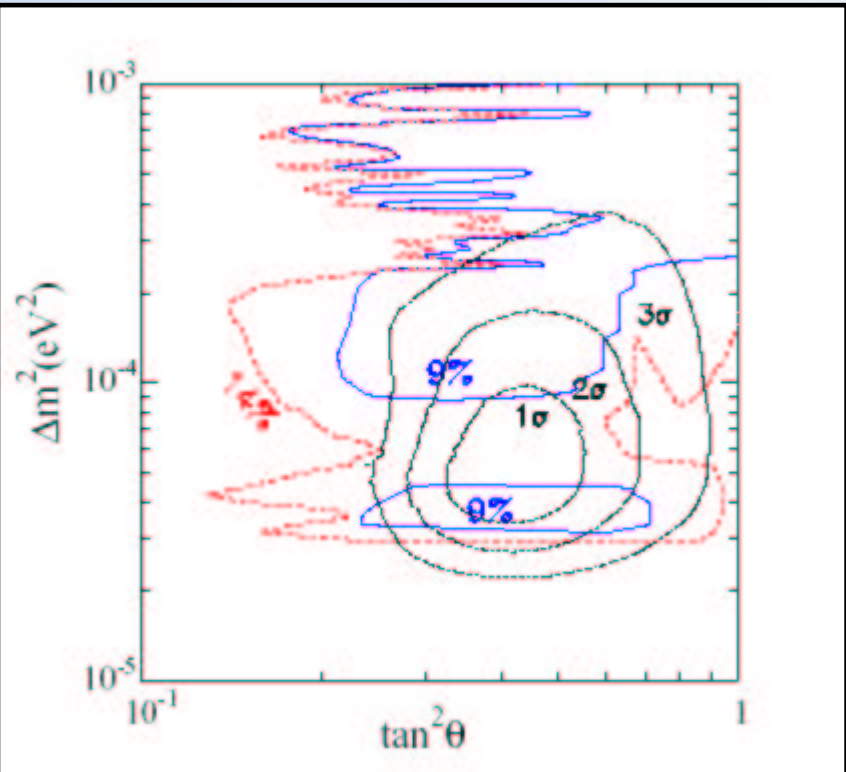
Combining KamLAND & SNO

- SNO provides an independent measure of the active content, but no constraint on the flux.
- KamLAND only reveals information about the mixing parameters, but not on the total active flux.
- Combining the two experiments provide an independent check on the active and sterile components

$$\delta f_B = \pm 12.5\%$$

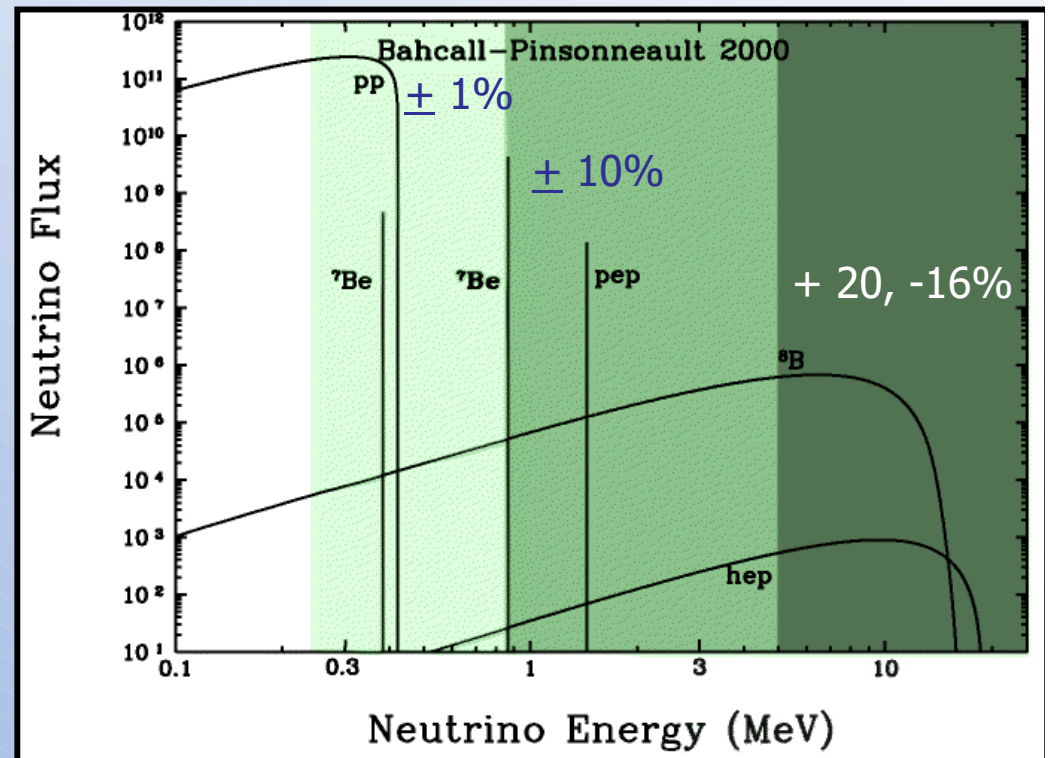
- If SNO improves NC measurement, this uncertainty will decrease even further
- Solar model independent.

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Precision Solar pp Measurements

- If one is able to access pp neutrinos from the sun, model is known extremely well.
- Limit there stems from detector uncertainties
- Need a dedicated experiment to probe this region and test both solar physics and steriles



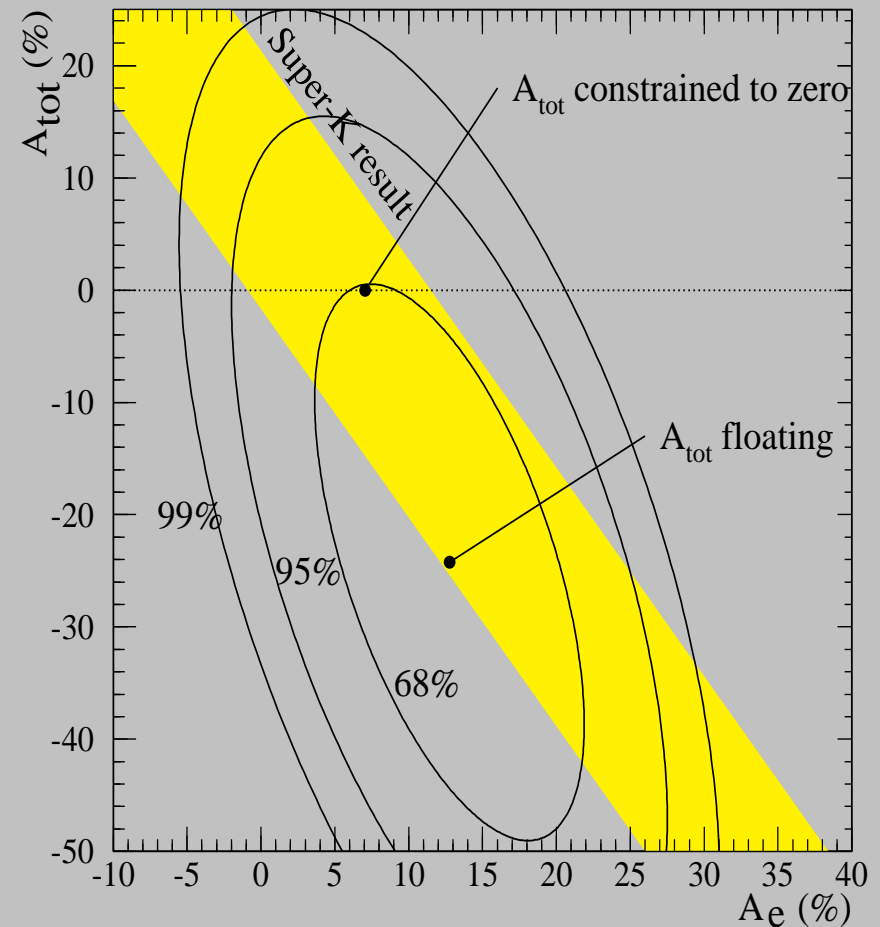
Day, Night, and Steriles?

- One can use day and night rates for neutral current rates in the sun in order to limit sterile neutrinos.
- Void of solar model systematic uncertainties
- Results consistent with no sterile content at 1.5σ level.

Signal Extraction in Φ_{CC} , Φ_{NC} , Φ_{ES}

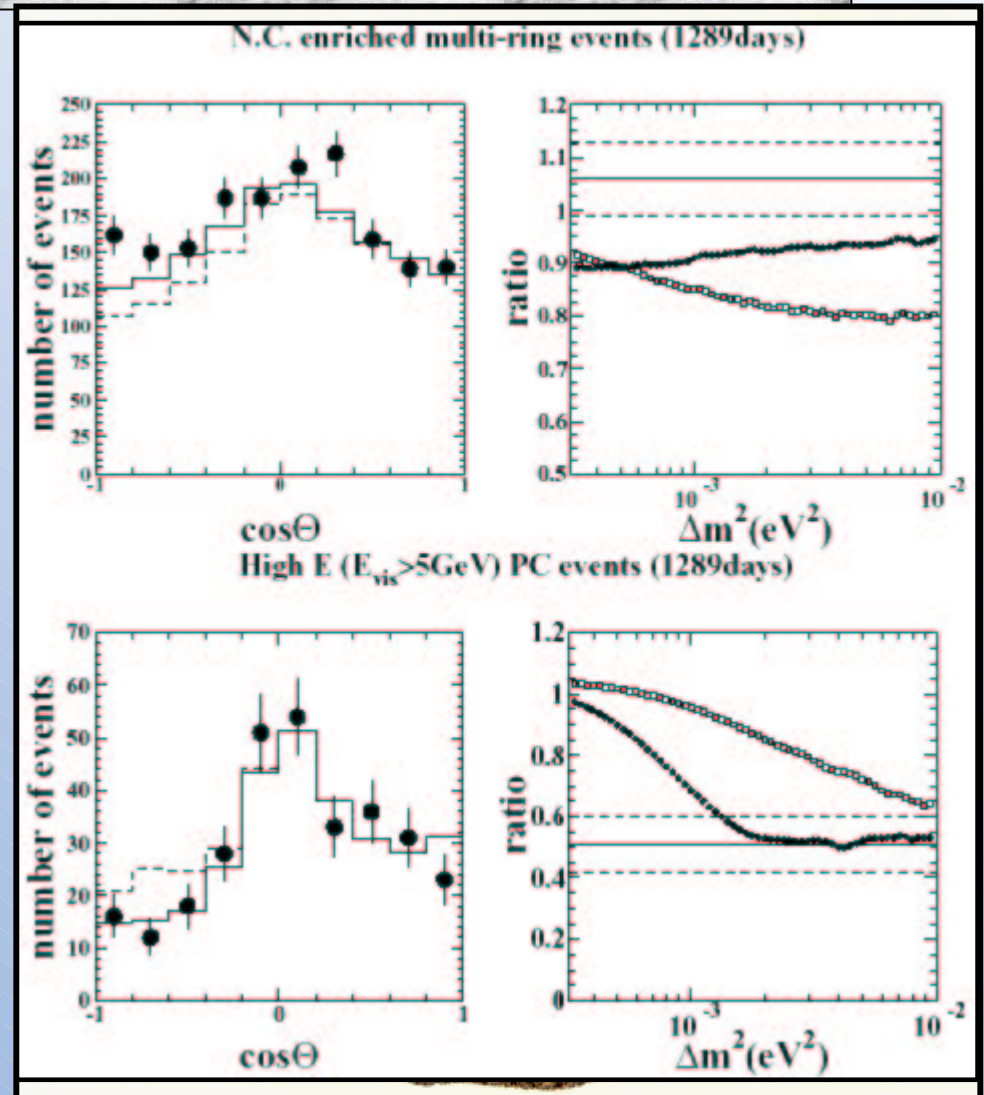
$$A_{CC}^{SNO} = 14.0 \pm 6.3 \%$$

$$A_{NC}^{SNO} = -20.4 \pm 16.9 \%$$



Steriles with SK

- Also look at neutral current (active) portion of atmospheric neutrinos
- Look for deficit in neutral current (π^0 ring)
- Rule out pure mixing to steriles in favor of mixing to ν_τ

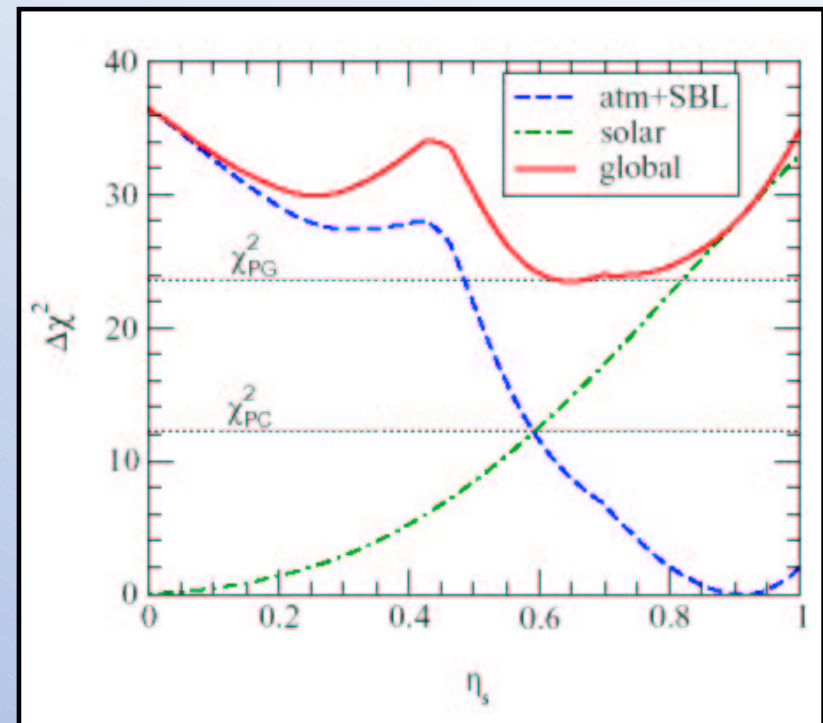


Do the Models Survive?

- **2+2 Model:**
 - Model gives prediction for solar and atmospheric constraints

$$P_{\text{solar}} + P_{\text{atmo}} = 1$$

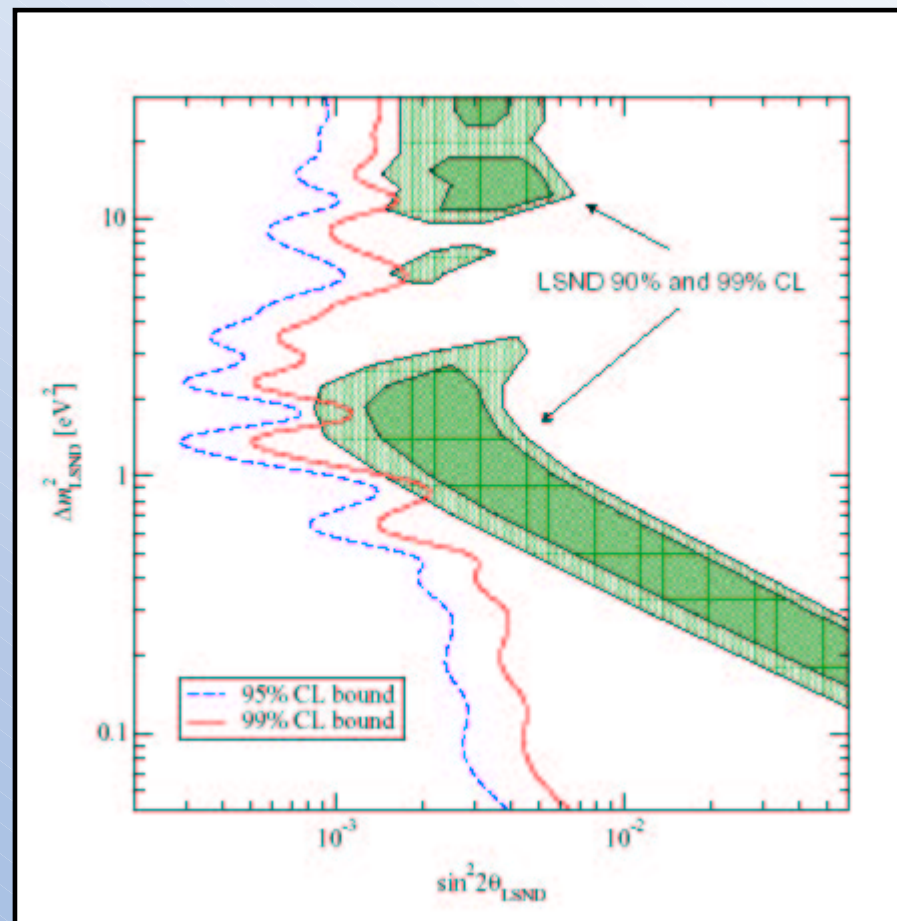
- New data now available:
 - SNO's neutral current measurement
 - Recent data analysis from SK
 - Updated numbers from the LSND collaboration on oscillation parameters



M. Maltoni, T. Schwetz, M. Tortola, J. Valle
hep/ph 0209368

Do the Models Survive?

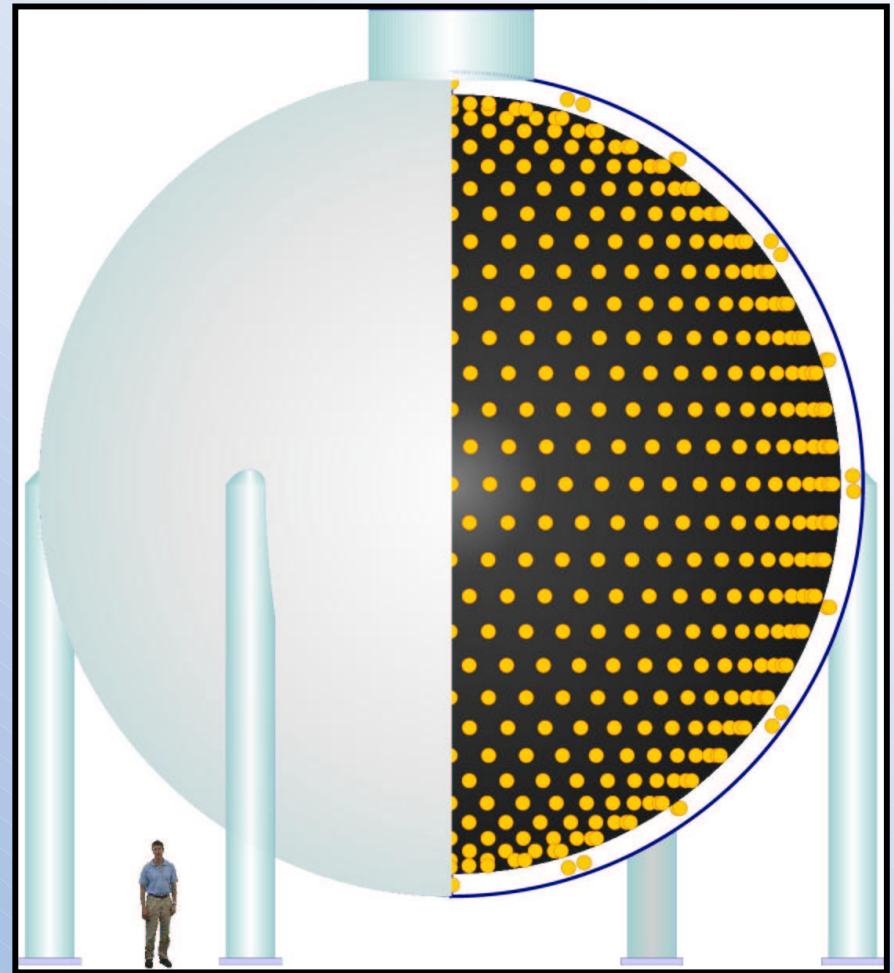
- **3+1 Model:**
 - Model usually disfavored due to restrictions from reactor limits
 - New oscillation probability from LSND recent analysis places more favor on the 3+1 scheme
 - But be careful...
 - Treatment of assumptions and systematics
 - For excellent treatment of systematics, see Fogli et. Al.



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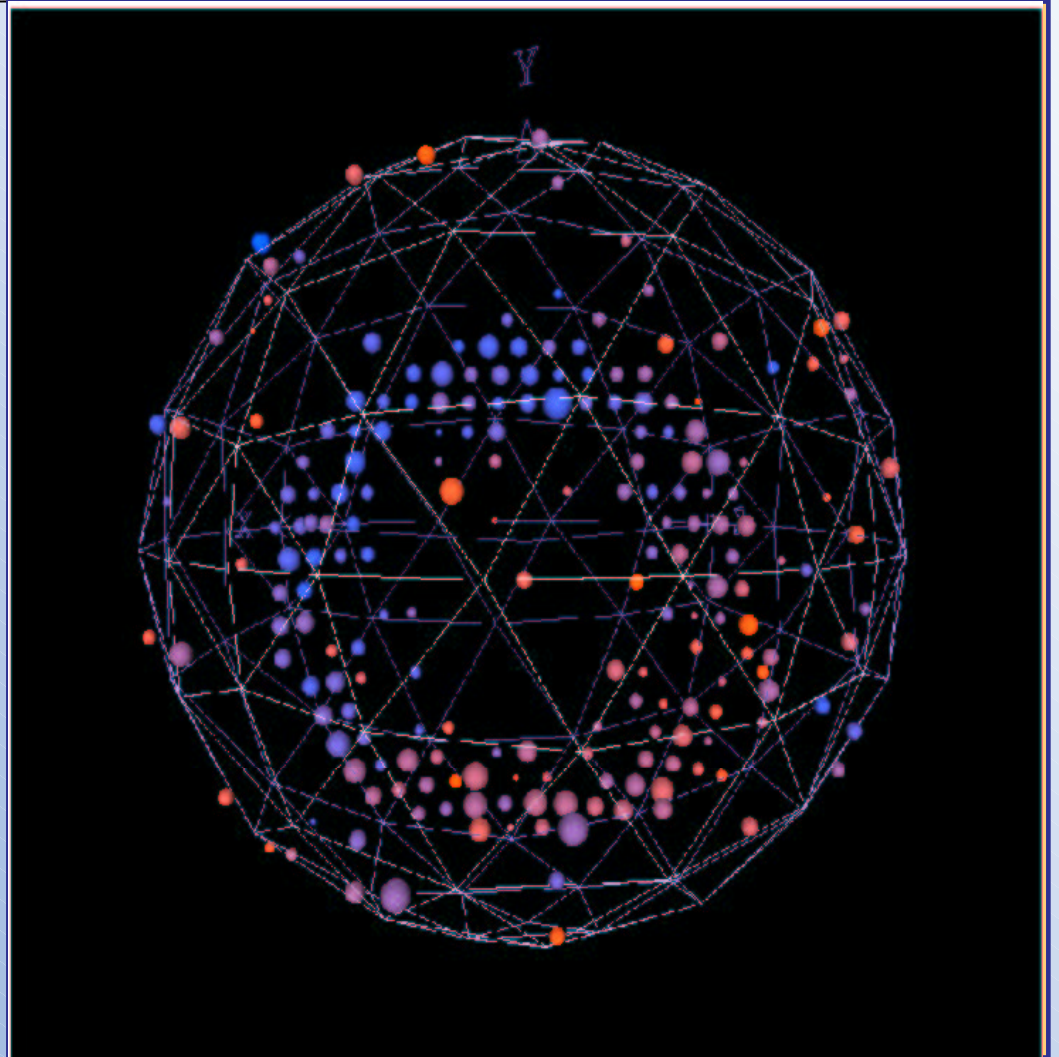
The MiniBooNE Experiment

- MiniBooNE experiment, in tradition with other oscillation experiments, is out to verify or refute the LSND signal
- Short baseline of ~ 1 GeV neutrino energy
- Probes same physics but with completely different systematics



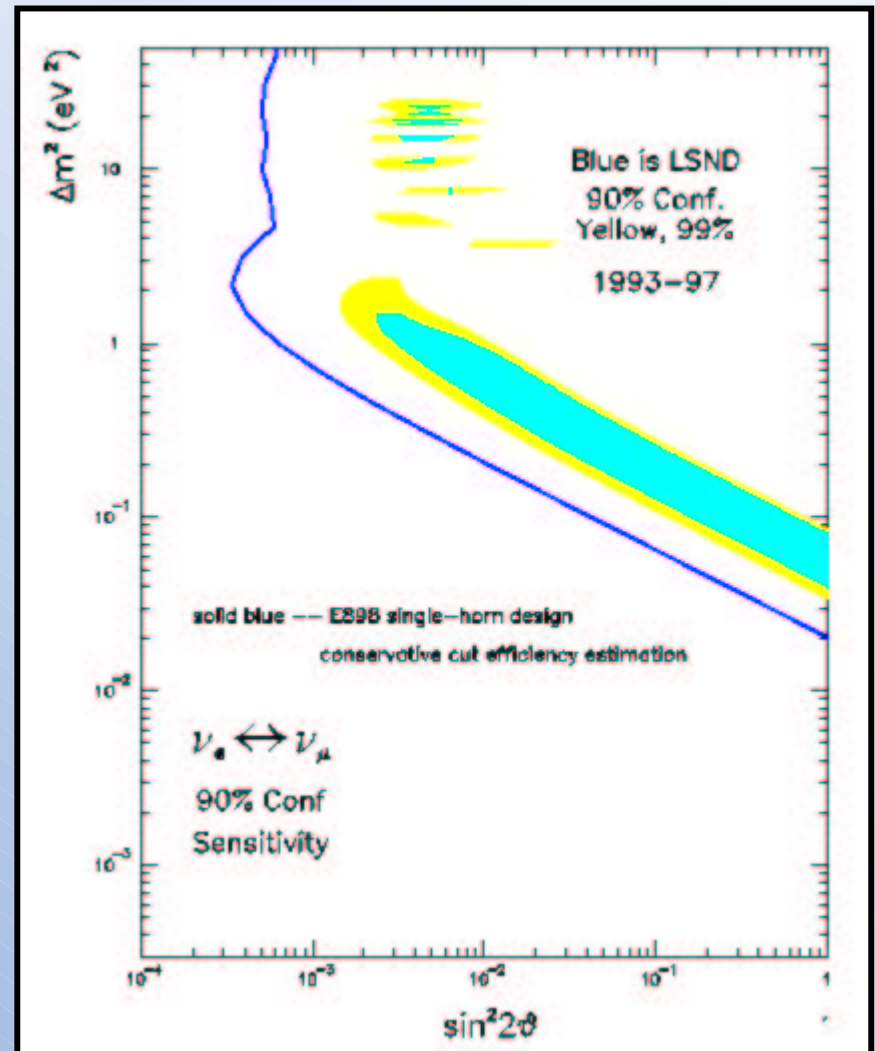
First Data

- MiniBooNE live and active
- First neutrino events from beam seen in detector
- Data taking for 1-2 years in neutrino and antineutrino modes



What to Expect

- If MiniBooNE sees a signal in neutrino running:
 - Confirmation of LSND
 - Is a single sterile compatible with rest of oscillation data?
- If MiniBooNE sees a signal only in anti-neutrino running:
 - CPT violation a reality?
 - What other systems test this scenario (KamLAND & SNO)?



- What to Conclude?

- Steriles provide an attractive addition to the Standard Model
- Experimental motivation from LSND provides a challenge to the framework
- Independent checks using different systematics is key to confirming or probing sterile neutrinos
- Exciting data from MiniBooNE and KamLAND to come!

